

PLOTTING AND INTERPRETTING GRAPHS

Year 9

Key Concept

Substitution – This is where you replace a number with a letter If a = 5 and b = 2

a + b =	5 + 2 = 7
a – b =	5 – 2 = 3
3a =	3 × 5 = 15
ab =	5 × 2 = 10
a ² =	5 ² = 25

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Clip Numbers 206 - 210, 251

Key Words

Intercept: Where two graphs cross. Gradient: This describes the steepness of the line. y-intercept: Where the graph crosses the yaxis. Linear: A linear graph is a straight line. Quadratic: A quadratic graph is curved, u or n

Tip Parallel lines have the same gradient.

shape.

Formula

 $Gradient = \frac{difference in y's}{difference in x's}$



Year 9

STRAIGHT LINE GRAPHS AND EQUATION OF A LINE

Key Concepts

Coordinates in 2D are written as follows:

x is the y is the value that (x, y)value is to the that is to left/right up/down Straight line graphs always have the equation: y = mx + c*m* is the **gradient** i.e. the steepness of the graph. c is the **y intercept** i.e. where the graph cuts the y axis.





Year 9 SIMULTANEOUS EQUATIONS

Simultaneous equations are when more than one equation are given, which involve more than one variable. The variables have the same value in each equation.

Quadratic

Key Concepts imultaneous quations are vhen more than ne equation are iven, which nvolve more than ne variable. The ariables have the ame value in ach equation.	wo linear equations: $3x + 2y = 18$ $3x - y = 9 \times 2$ $3x + 2y = 18$ $6x - 2y = 18 + D^{SS}$ $9x = 36$ $x = 4$ $9x = 36$ $x = 4$ $3x + 2y = 18$ $3x + 2y = 18$ $12 + 2y = 18$ $12 + 2y = 18$ $2y = 6$ $y = 3$	One linear and one quadratic equation: Examples $x^2 + y^2 = 17$ y = x - 3 Substitute $y = x - 3$ into y in the quadratic equation. $x^2 + (x - 3)^2 = 17$ $x^2 + x^2 - 6x + 9 - 17 = 0$ $2x^2 - 6x - 8 = 0$ Solve by factorising or using the quadratic formula. x = 4 or x = -1 Substitute the x values into the linear equation to find the corresponding y values. When x = 4, $y = 4 - 3 = 1When x = -1$, $y = -1 - 3 = -4$
A hegartymaths	Key Words	Solve each set of simultaneous equations:
190-195	Substitution Elimination Linear	1) $3x + 2y = 4$ 4x + 5y = 17 2) $x^2 + y^2 = 13$ x = y - 5

 $\xi = x pup \zeta = \chi \gamma z = x pup \xi = \chi (\zeta \zeta z = \gamma pup \zeta = x (\zeta z = \gamma qup \zeta = x))$



Year 9 SOLVE SIMULTANEOUS EQUATIONS GRAPHICALLY

Key Concepts

Simultaneous equations are when more than one equation are given which involve more than one variable. The variables have the **same** value in each equation.

Simultaneous equations can be solved graphically whereby the intersection of the graphs gives the x and *y* values.

259

Solve graphically: $y = x^2$ Solve graphically: y = 2x + 1Examples y = x + 2y = -x + 4 $y = x^2$ v = 2x + 1x = -1 and y = 1x = 2 and y = 4y = -x + 4x = 1 and y = 31) 2) & hegartymaths Key Words Solve each set of Simultaneous simultaneous equations Equation graphically. Intersection $\lambda = \chi$ bub $\lambda = 0$ and $\gamma = \chi$ is $\lambda = 0$ and $\gamma = \chi$ is $\lambda = \chi$ is a second with the second secon







Year 9 **INTRODUCING PROBABILITY**

Key Concept

Chance



Probabilities can be written as:

- Fractions
- Decimals
- Percentages

A hegartymaths **Clip Numbers** 349 - 359

Key Words Probability: The chance of something happening as a numerical value. Impossible: The outcome cannot

happen. **Certain:** The outcome will definitely happen. **Even chance:** The are two different outcomes each with the same chance of happening. Expectation: The amount of times you expect an outcome to happen based on probability.

Tip Probabilities always add up to 1.

Formula *Expectation* = *Probability* \times *no. of trials*

Examples



1) What is the probability that a bead chosen will

Show the answer on a number line.

 $Probability = \frac{Number of favourable outcomes}{\pi}$ Total number of outcomes

$$P(Yellow) = \frac{2}{8} = \frac{1}{4}$$

2) How many **yellow** beads would you **expect** if you pulled a bead out and replaced it 40 times?

 $\frac{1}{4} \times 40 = \frac{1}{4} of 40 = 10$

Questions

In a bag of skittles there are 12 red, 9 yellow, 6 blue and 3 purple left. Find: a) P(Red) b) P(Yellow) c) P(Red or purple) d) P(Green)

O (b $\frac{1}{2} = \frac{21}{00}$ (c) $\frac{1}{00} = \frac{1}{00} = \frac{1}{00}$ (c) $\frac{1}{2} = \frac{1}{0}$ (c) $\frac{1}{2}$ (c) $\frac{1}{2} = \frac{1}{0}$ (c) $\frac{1}{2}$ (c) $\frac{1}{2} = \frac{1}{0}$ (c) $\frac{1}{2}$ (c) $\frac{1}{2}$



Year 9 **THEORETICAL PROBABILITY**

Key Concepts

Probabilities can be described using words and numerically.

We can use fractions, decimals or percentages to represent a probability.

Theoretical probability is what should happen if all variables were fair.

All probabilities must add to 1.

The probability of something NOT happening equals:

1 - (probability of it happening)

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349-353

Probability	LNaill			
Impossible	E	ven chance	2	Certain
0	1	<u>1</u>	3	4
4	4	2	4	4
0	0.25	0.5	0.75	1
0%	25 %	50 %	75 %	100%

There are only red counters, blue counters, white counters and black counters in a bag.

Colour	Red	Blue	Black	White
No. of counters	9	3	5	2

- 1) What is the probability that a blue counter is chosen? $\frac{3}{19} = \frac{number \ of \ blue}{total \ number \ of \ counters}$ 2) What is the probability that red is **not** chosen? $\frac{10}{19} = \frac{number of all other colours}{total number of counters}$

Examples

There are only red counters, blue counters, white counters and black counters in a bag.

Colour	Red	Blue	Black	White
No. of counters	9	3 <i>x</i>	<i>x</i> -5	2 <i>x</i>

A counter is chosen at random, the probability it is red is $\frac{9}{100}$. Work out the probability is black. 9 + 3x + x - 5 + 2x = 1006x + 4 = 100x = 16Number of black counters = 16 - 5= 11 Probability of choosing black = $\frac{11}{100}$

Key Words Theoretical Probability

Fraction

Decimal

Percentage

Certain Impossible Even chance

	1	2	3
Prob	5	4	9

1a) Calculate the probability of choosing a 2. b) Calculate the probability of not choosing a 3.

	1	2	3	
Prob	0.37	2 <i>x</i>	x	

2) Calculate the probability of choosing a 2 or a 3.

12.0 = (5) + 24.0 = (2) + (2



Year 9 RELATIVE FREQUENCY

Key Concepts

Experimental probability differs to theoretical probability in that it is based upon the **outcomes from experiments**. It may not reflect the outcomes we expect.

Experimental probability is also known as the **relative frequency** of an event occurring.

Estimating the number of times an event will occur:

Probability × no. of trials

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Colour	red	blue	white	black
Prob	x	0.2	0.3	x

A spinner is spun, it has four colours on it.

The relative frequencies of each colour are recorded.

The relative frequency of red and black are the same.

a) What is the relative frequency of red?

1 - (0.2 + 0.3) = 0.5 $x = \frac{0.5}{2} = 0.25$

b) If the spinner is spun 300 times, how many times do you expect it to land on white? $0.3 \times 300 = 90$

Key Words Experimental Relative frequency Fraction Decimal Probability Estimate

Number	1	2	3	4	a)
Prob	x	0.46	0.28	x	

A spinner is spun which has 1,2,3,4 on it. The probability that a 1 and a 4 are spun are equal.

- What is the probability that a 4 is landed on?
- If the spinner is spun 500 times how many times do we expect it to land on a 2?

b)

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LISTING OUTCOMES AND SAMPLE SPACE

Year 9

Key Concepts	\bigcap		Exan	nples	5						
When there are a number of different possible outcomes in a situation we need a logical and systematic way in which to view them all		Starter Main Two dice are thrown and the possible outcomes are shown the sample space diagram below:						are shown in			
						1	2	3	4	5	6
		Fishcake	Lasagne		1	(1,1)	(1,2)	(1,3)	(1,4)	(1,5)	(1,6)
			Beef		2	(2,1)	(2,2)	(2,3)	(2,4)	(2,5)	(2,6)
		wieion	Salmon		3	(3,1)	(3,2)	(3,3)	(3,4)	(3,5)	(3,6)
We can be asked to list all			Samon		4	(4,1)	(4,2)	(4,3)	(4,4)	(4,5)	(4,6)
possible outcomes e.g.					5	(5,1)	(5,2)	(5,3)	(5,4)	(5,5)	(5,6)
choices from a menu,		List all of the combi	nations possible		6	(6,1)	(6,2)	(6,3)	(6,4)	(6,5)	(6,6)
order in which people finish a race.		when one starter and one main are chosen. F. L M. L		1) What is the probability that 2 numbers which are the same are rolled?							
We can also use a sample		, F, В	, З М, В	$\frac{6}{26} = \frac{6}{1000}$ total numbers of outcomes							
space diagram. This		F, S	S M, S		2) What is the probability that two even numbers						
records the possible		lote: You can write the initials of each			are rolled?						
outcomes of two different	(option in a test. You do not need to write			$\frac{9}{1} = \frac{outcomes where numbers are both even}{1}$						
events happening.		out the full word.		36 total number of outcomes							
been turnethe	$\boldsymbol{\mathcal{C}}$									2a) V	/hat is the
		Key Words	1) Abe, Ben and Carl				Spinner probability		ability that a		
		List	of the options for the order that the boys can end the race.	Coin		Red	Gre	een	Blue	head	is landed on?
358-359 <i>,</i> 370-371	Outcor Samp spac Probab	Outcome			Heads	нв	Н	G	нв	b) Wl	hat is the
		Sample			Toile			,0	т.р	probability that a	
		space			Tails	I,R	ļ I,	,0	т,в	are la	and a green
		Probability									
		·			⁹ _∓ (q	<u>9</u> (ег	AB, CBA	d2 (A28	, BAC, E	BC, ACB	а (1 :2яэw2na



TWO WAY TABLES AND PROBABILITY TABLES

Year 9

Key Concepts

Two way tables are used to tabulate a number of pieces of information.

Probabilities can be formulated easily from two way tables.

Probabilities can be written as a **fraction, decimal or a percentage** however we often work with fractions. You do not need to simplify your fractions in probabilities.

Estimating the number of times an event will occur Probability × no. of trials

A hegartymaths

353, 422-424

LAII							
There are only red counters, blue counters, white counters and black counters in a bag.							
Colour	Red	Blue	Black	White			
No. of counters	9	3 <i>x</i>	<i>x</i> -5	2 <i>x</i>			
A counter is chosen at random, the probability it is red is $\frac{9}{100}$. Work out the probability is black.							
9 + 3x + x - 5 + 2x = 100 $6x + 4 = 100$							

x = 16

= 11

Examples

80 children went on a school trip. They went to London or to York.

23 boys and 19 girls went to London. 14 boys went to York.

	London	York	Total	
Girls	19	24	43	
Boys	23	14	37	
Total	42	38	80	

What is the probability that a person is chosen that went to London? $\frac{42}{80}$ If a girl is chosen, what is the probability that she went to York? $\frac{24}{38}$

Key Words Two way table Probability Fraction Outcomes Frequency

Number of black counters = 16 - 5

Probability of choosing black = $\frac{11}{100}$

	1	2	3	
Prob	0.37	2 <i>x</i>	x	

1a) Calculate the probability of choosing a 2 or a 3.b) Estimate the number of times a 2 will be chosen if the experiment is repeated 300 times.

2a) Complete the two way table:

		Total		
	9	10	11	
Boys			125	407
Girls		123		
Total	303	256		831

b) What is the probability that a Y10 is chosen, given that they are a girl .





Year 9

PROBABILITY TREE DIAGRAMS

Key Concepts

Independent events are events which do not affect one another.

Dependent events affect one another's probabilities. This is also known as **conditional probability**.

We **multiply** two probabilities when one event follows another. **Examples**There are red and blue counters in a bag.The probability that a red counter is chosen is $\frac{2}{9}$.A counter is chosen and **replaced**, then a second counter is chosen.Draw a tree diagram and calculate the probability that two counters of the same colour are chosen.



A hegartymaths 361-362, 364, 368-369

Key Words Independent Dependant Conditional Probability Fraction Multiply There are blue and green pens in a drawer.

There are 4 blues and 7 greens.

A pen is chosen and then **replaced**, then a second pen is chosen. Draw a tree diagram to show this information and calculate the probability that pens of different colours are chosen.

ANSWERS: 56/121



Year 9 VENN DIAGRAMS

Key Concepts

Venn diagrams show all possible relationships between different sets of data.

Probabilities can be derived from Venn diagrams. Specific notation is used for this:

 $P(A \cap B) = Probability of A and B$

 $P(A \cup B) = Probability of A or B$

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P(A') = Probability of not A
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A hegartymaths 372-388, 391

Key Words Venn diagram Union Intersection Probability Outcomes



40 students were surveyed:

20 have visited France15 have visited Spain10 have visited both France and Spain

Example

a) Complete the Venn diagram

b) Calculate:



- a) Complete a Venn diagram to represent this information.
- b) Calculate:

i) $P(F \cap S)$ ii) $P(F \cup S)$ iii) P(S')

iv) The probability someone who has visited France, has not gone to Spain.

ANSWERS: bi) 10/40 ii) 25/40 iii) 25/40 iv) 20/40 = 1/2